

# Angles

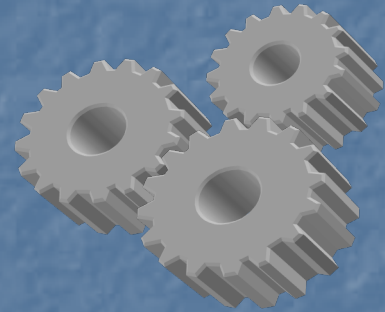
The basics

# Introduction

- Angles will be used in virtually every chapter in Geometry this year. It is very important to know the basics of angles before moving into further chapters.

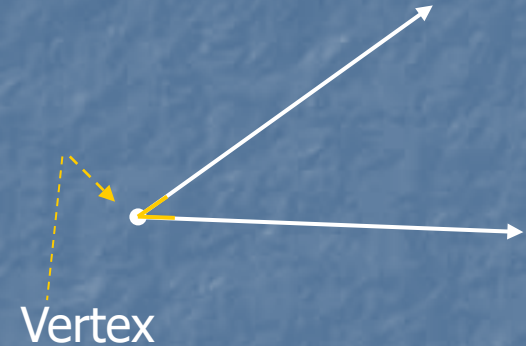
# Topics of Discussion

- Angle parts
- Types of angles
- Relationships between angles
- Angle Addition Postulate



# Angle Parts

- An angle is a figure formed by two rays with the same endpoint.
- The common endpoint is called the vertex of the angle.
- Each of the rays is a side of the angle.

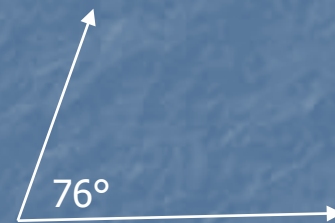
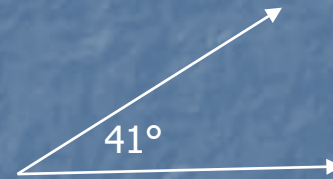




# Measure of an Angle

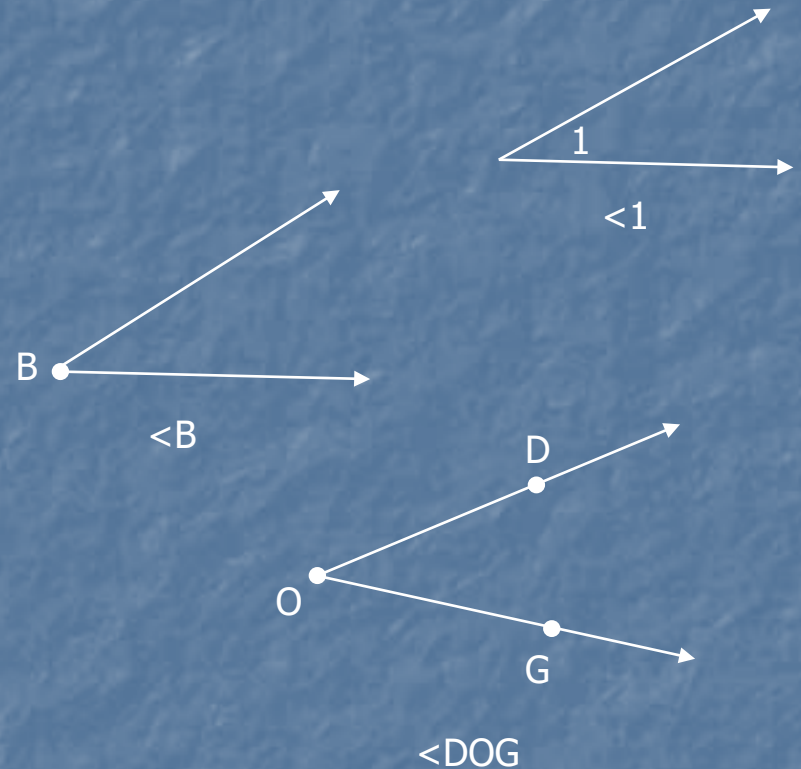


- An angle is measured in units called degrees.
- The more the two rays are separated from each other, the greater the angle will be.
  - to describe the measure of an angle we would say:  
 $m\angle 1 = 22^\circ$



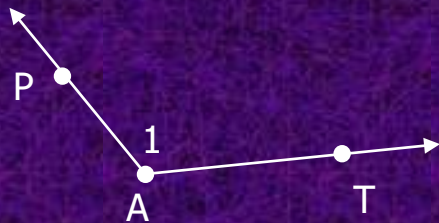
# Naming the Angle

- An Angle can be named in one of three ways
  - A number assigned to it
  - It can be named after its vertex (if there is only one angle at that point)
  - Using three points on the angle (one from each side, and the middle vertex)



# Give four names for each angle

1.)



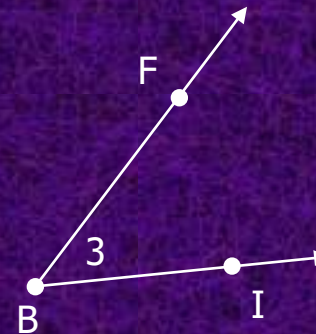
$\angle PAT$

$\angle A$

$\angle 1$

$\angle TAP$

2.)



$\angle FBI$

$\angle 3$

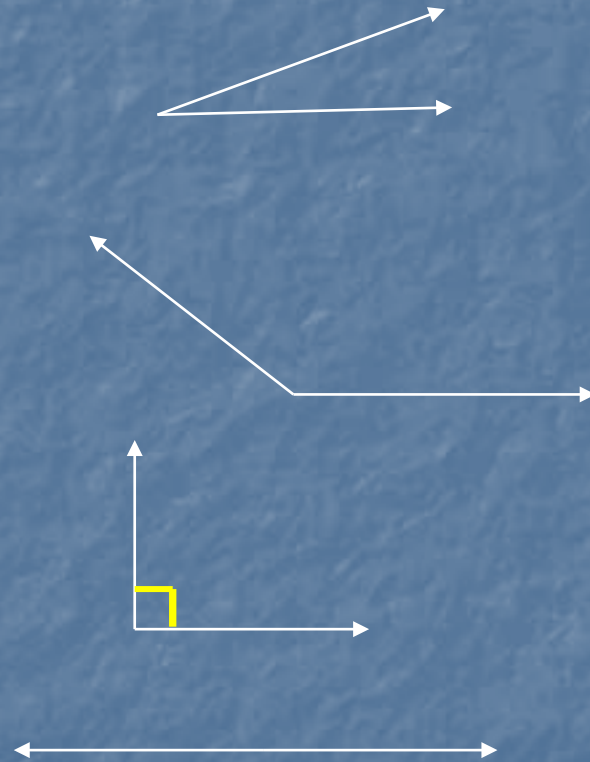
$\angle B$

$\angle IBF$

\*\*note: the numbers here are used to name the angle. If it were meant to show the measure, it would have a degree symbol.

# Types of Angles

- Angles are classified by their measure
  - Acute angles are less than  $90^\circ$
  - Obtuse angles are greater than  $90^\circ$
  - Right angles are exactly  $90^\circ$
  - Straight angles are  $180^\circ$





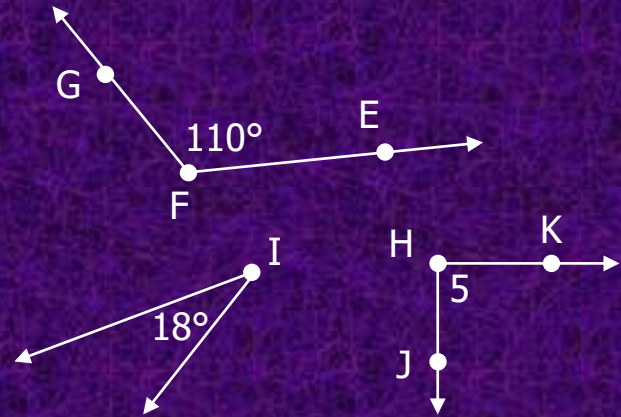
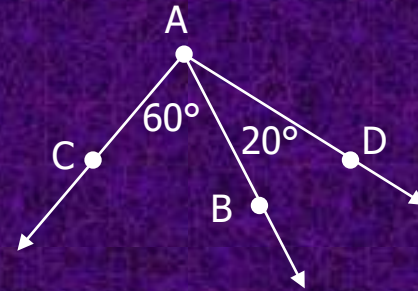
# Types of Angles

Acute angle  
Right angle  
Obtuse angle



# Fill in the blanks using the figures.

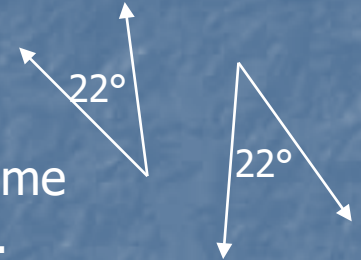
- $m\angle BAC = \underline{60^\circ}$
- Two names for the obtuse angle are  $\underline{\angle F}$  and  $\underline{\angle GFE}$ .
- $\underline{m\angle I} = 18^\circ$
- Two other names for  $\angle H$  are  $\underline{\angle 5}$  and  $\underline{\angle JHK}$
- $m\angle DAC = \underline{80^\circ}$



# Angle Relationships

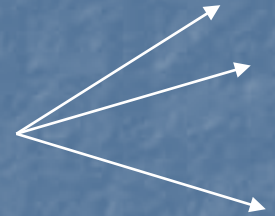
## ■ Congruent Angles

Angles that have the same measure are congruent.



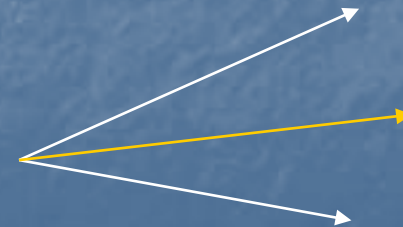
## ■ Adjacent Angles

Coplanar angles that have the same vertex and one common side are adjacent.



## ■ Bisector of an Angle

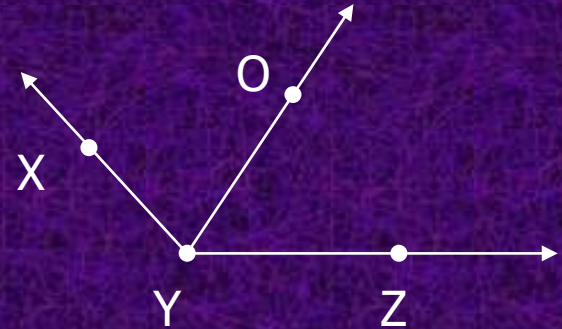
A ray that cuts an angle into two equally sized angles is a bisector.



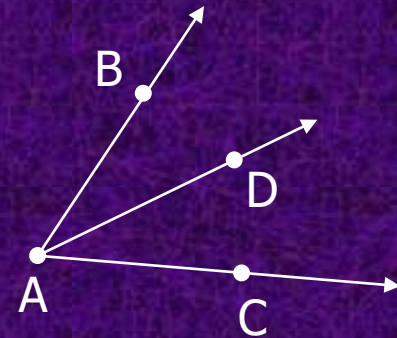
\*\*This forms two congruent and adjacent angles

# Solve:

1.) If  $m\angle XYZ = 122^\circ$ , and  $\overrightarrow{YO}$  is a bisector of  $\angle XYZ$ , then  $m\angle OYZ = \underline{61^\circ}$ .

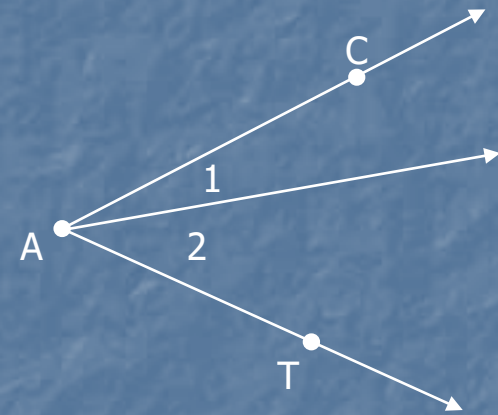


2.) If  $\overrightarrow{AD}$  is a bisector of  $\angle BAC$ , and  $m\angle BAD = 32^\circ$ , then  $m\angle DAC = \underline{32^\circ}$ , and  $m\angle BAC = \underline{64^\circ}$ .



# Angle Addition Postulate

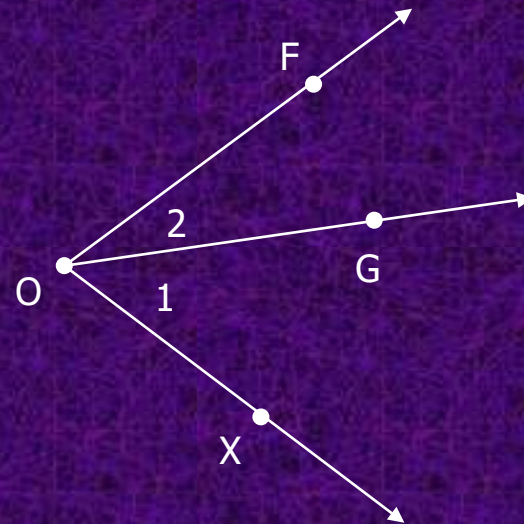
- The Angle Addition Postulate states that if we have two adjacent angles, then the sum of the two small angles formed will be equal to the larger angle.
- The pieces add up to the whole.



$$m\angle 1 + m\angle 2 = m\angle CAT$$

# Find the value of $x$

- If  $m\angle 1 = 28^\circ$ , and  $m\angle 2 = 37^\circ$ , then  $m\angle FOX = \underline{65^\circ}$ .
- If  $m\angle 2 = 37^\circ$ , and  $m\angle FOX = 77^\circ$ , then  $m\angle 1 = \underline{40^\circ}$ .
- If  $m\angle GOX = 45^\circ$ , and  $m\angle XOF = 80^\circ$ , then  $m\angle 2 = \underline{35^\circ}$ .



# Summary

- Angles are formed by intersecting rays.
- Angles are named in three ways.
- There are three main types of angles we will use.
- Special angle relationships exist that show connection between angles.